## OSCILLATIONS OF DIFFERENCE EQUATIONS WITH SEVERAL DEVIATING ARGUMENTS

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## ABSTRACT

Sufficient conditions for the oscillation of all solutions to the retarded difference equation

$$\Delta x(n) + \sum_{i=1}^{m} p_i(n) x(\tau_i(n)) = 0, \quad n \ge 0,$$

and the (dual) advanced difference equation

$$\nabla x(n) - \sum_{i=1}^{m} p_i(n) x(\sigma_i(n)) = 0, \quad n \ge 1,$$

where  $(p_i(n))$ ,  $1 \leq i \leq m$  are sequences of nonnegative real numbers,  $(\tau_i(n))$ ,  $1 \leq i \leq m$  are sequences of integers such that

 $\tau_i(n) \le n-1 \quad \forall n \ge 0, \quad \text{and} \quad \lim_{n \to \infty} \tau_i(n) = \infty, \quad 1 \le i \le m,$ 

 $(\sigma_i(n)), 1 \leq i \leq m$  are sequences of integers such that

$$\sigma_i(n) \ge n+1 \quad \forall n \ge 1, \quad 1 \le i \le m,$$

 $\Delta$  denotes the forward difference operator  $\Delta x(n) = x(n+1) - x(n)$  and  $\nabla$  denotes the backward difference operator  $\nabla x(n) = x(n) - x(n-1)$ , are established. Examples illustrating the results are also given.