

Homeworks 13 and 14

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Molecular Symmetries- General Theory

The concept of symmetry is everywhere, and molecules are no exception. If we think about the structure of a molecule (like the one in the picture below), there are some symmetry operations that we can immediately see, such as the 120° rotations by the axis passing through the boron in the example below. And, for each existing symmetry operation in a certain molecule we associate a symmetry element, which may be an axis, a plane, a line or even a point. For example, rotations by the axis passing through the boron in the molecule below would have the same symmetry element. The possible types of symmetry elements a molecule may have are:

1. **Identity (E)**: The identity operation leaves the molecule unchanged, thus the symmetry element is the entire molecule. All molecules have this element, which serves as the identity of the symmetry group.

2. **n-fold axis of rotation (C_n)**: A molecule has rotational symmetry if it can be rotated by $\frac{360^\circ}{n}$ around a symmetry axis and remain unchanged. Molecules may have more than one axis of rotation, and rotations, are, by convention, counterclockwise.

3. **Plane of Symmetry (σ)**: A molecule possesses a plane of symmetry if it remains unchanged by a reflection on said plane. Reflection planes can be of the following types:

- Vertical planes (σ_v): Contain the axis of rotation.
- Horizontal planes (σ_h): Are perpendicular to the axis of rotation.
- Dihedral mirror planes (σ_d): Bisect the angles between two C_2 axes.

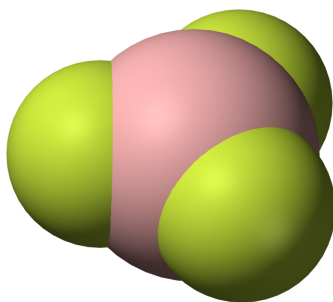
4. **Center of symmetry (i)**: A molecule possesses a center of symmetry if when inverting by said center the molecule remains unchanged.

5. **n- fold improper rotation axis (S_n)**: Consists of combining a rotation around an axis with a reflection through a plane perpendicular to the axis.

Molecules may be divided into different **molecular point groups**, based on which

symmetry elements they possess. As a curiosity, there are 15 different molecular point groups, such as, for example, D_{nh} which contains all molecules with: identity, an n -fold axis of rotation, n 2-fold axis of rotation perpendicular to the principal one, n vertical mirror planes and an horizontal mirror plane.

Example: Boron Trifluoride (BF_3)



Boron trifluoride is a planar molecule, so it is fair to representing using just a plane. The symmetry elements of BF_3 are:

- A principal C_3 axis passing through the boron atom and perpendicular to the molecular plane.
- Three C_2 axes passing through the boron atom and bisecting the angles between the fluorine atoms.
- A horizontal plane of reflection (σ_h) coinciding with the molecular plane.
- Three vertical planes of reflection (σ_v), each containing the C_3 axis and one fluorine atom.

A visual clarification for this symmetries may be found on the end of the paper. Based on these elements, BF_3 belongs to the D_{3h} point group.

Applications

One may ask why this theory is relevant for chemistry. Well, studying the symmetries of molecules is, indeed, useful. I won't go into further detail, but here are some of the possible applications of this theory:

1. Predicting whether a molecule will be polar or chiral;
2. Visualization of molecular orbits;

3. Examination of chemical bonding;
4. Investigation of the vibrational motions of a given molecule.

